

MODEL QUESTION PAPER
MATHEMATICS PAPER I (A)
 (Algebra, Vector Algebra and Trigonometry)
 (English Version)

Time: 3 Hrs.

Max. Marks. 75

Note : Question paper consists of 'Three' Sections A, B and C.

SECTION - A

I. Very short answer questions 10 x 2 = 20 Marks
 (Attempt all questions)
 (each question carries 'Two' marks)

01. Find the domain of the real valued functions $f(x) = \sqrt{9-x^2}$
02. In $\triangle ABC$, D is the mid point of BC. Express $\overline{AB} + \overline{AC}$ in terms of \overline{AD}
03. Find the vector equation of the line through the points $2\vec{i} + \vec{j} + 3\vec{k}$ and $-4\vec{i} + 3\vec{j} - \vec{k}$
04. If $\vec{a} = \vec{i} + 2\vec{j} + 3\vec{k}$ and $\vec{b} = 3\vec{i} - \vec{j} + 2\vec{k}$, then find the angle between $(2\vec{a} + \vec{b})$ and $(\vec{a} + 2\vec{b})$
05. Sketch the graph of $\sin x$ in $(0, 2\pi)$
06. Find the value of $\cos^2 45^\circ - \sin^2 15^\circ$
07. Show that $\cos h(3x) = 4 \cos h^3 X - 3 \cos hx$.
08. If $c^2 = a^2 + b^2$, write the value of $4s(s-a)(s-b)(s-c)$ in terms of a and b .
09. Simplify
$$\frac{(\cos q - i \sin q)^7}{(\sin 2\theta - i \cos 2\theta)^4}$$
10. Expand $\cos 4\theta$ in powers of $\cos \theta$

SECTION - B

II. Short answer questions. Attempt five questions 5 x 4 = 20 marks

11. $f : A \rightarrow B, g : B \rightarrow C$;
 $f = \{(1, a), (2, c), (4, d), (3, d)\}$
 and $g^{-1} = \{(2, a), (4, b), (1, c), (3, d)\}$
 then compute $(g \circ f)^{-1}$ and $f^{-1} \circ g^{-1}$.
12. Find the cube root of $37 - 30\sqrt{3}$.
13. If $x = 1 + \log_a bc, y = 1 + \log_b ca$ and $z = 1 + \log_c ab$, then show that $xyz = xy + yz + zx$.
14. By vector method, prove that the diagonals of a parallelogram bisect each other.
15. Find the area of the triangle formed with the points $A(1, 2, 3), B(2, 3, 1)$ and $C(3, 1, 2)$ by vector method.
16. Find the solution set of the equation $1 + \sin 2\theta = 3 \sin \theta \cos \theta$
17. Show that $\sin^{-1}\left(\frac{3}{5}\right) + \sin^{-1}\left(\frac{8}{17}\right) = \sin^{-1}\left(\frac{77}{85}\right)$

SECTION - C

III. Long answer questions : (Attempt 'FIVE' questions) 5 x 7 = 35 marks

18. If $f : A \rightarrow B$ and $g : B \rightarrow C$ are bijections, then prove that $g \circ f : A \rightarrow C$ is also bijection.
19. Using the principle of Mathematical induction show that
$$1^2 + (1^2 + 2^2) + (1^2 + 2^2 + 3^2) + \dots \text{ upto } n \text{ terms} = \frac{n(n+1)^2(n+2)}{12}$$

MODEL QUESTION PAPER
MATHEMATICS PAPER - I (B)
 (Calculus and Co-ordinate Geometry)
 English Version

Time: 3 Hours

Max. Marks. 75

Note: Question paper consists of three sections A, B and C.

Section - A

(Very short answer type questions)

Attempt all questions :

10x2=20 marks

Each question carries two marks. ,

01. Write the condition that the equation $ax+by+c=0$ represents a non-vertical straight line. Also write its slope.
02. Transform the equation $4x-3y+ 12=0$ into slope-intercept form and intercept form of a straight line.
03. Find the ratio in which the point C (6,-17,-4) divides the line segment joining the points A(2,3,4) and B(3,-2,2)
04. Evaluate $\lim_{x \rightarrow 0} \frac{3x-1}{\sqrt{1+x} - 1}$
05. Evaluate $\lim_{x \rightarrow \infty} (\sqrt{x+1} - \sqrt{x})$
06. Find the constant 'a' so that the function f given by
 $f(x) = \sin x$ if $x \leq 0$
 $= x^2 + a$ if $0 < x < 1$ is continuous at $x=0$
07. Find the derivative of $\log_{10}x$ w.r.t x
08. If $Z = e^{ax} \sin by$ then find Z_{ny} .
09. If $y = x^2 + 3x + 6$, $x = 10$, $\Delta x = 0.01$, then find Δy and dy .
10. Find the interval in which $f(x) = x^3 - 3x^2$ is decreasing.

20. For any vector \vec{a} , \vec{b} ; and \vec{c} ,
 prove that $(\vec{a} \times \vec{b}) \times \vec{c} = (\vec{a} \cdot \vec{c}) \vec{b} - (\vec{b} \cdot \vec{c}) \vec{a}$

21. If $A + B + C = 180^\circ$, then show that
 $\sin 2A - \sin 2B + \sin 2C = 4 \cos A \sin B \cos C$

22. In ΔABC , show that

$$\frac{r_1}{bc} + \frac{r_2}{ca} + \frac{r_3}{ab} = \frac{1}{r} - \frac{1}{2R}$$

23. One end of the ladder is incontact 'with a wall and another end is in contact with the level ground making an angle ' α '. When the foot of the ladder is moved to a distance 'a' cms, the end in contact with the wall slides through 'b' cms. and the angle made by the ladder with the level ground is now ' β ', show that

$$a = b \tan \left(\frac{\alpha + \beta}{2} \right)$$

24. Reduce the complex numbers $3 + 4i$,

$$\frac{3}{4} (7+i) (1+i), \frac{2(i-18)}{(1+i)^2}, \frac{5(i-3)}{1+i}$$

to $x+iy$ form. Show that the four points represented by these complex numbers form a square in the argand plane.



Section - B
(Short answer type questions)

Attempt any five questions. Each question carries Four marks
5x4=20 marks

11. Find the equation of locus of a point, the sum of whose distances from (0, 2) and (0, -2) is 6 units
12. Show that the axes are to be rotated through an angle of $\frac{1}{2} \tan^{-1} \left(\frac{2h}{a-b} \right)$ so as to remove the xy term from the equation $ax^2 + 2hxy + by^2 = 0$ If $a \neq b$ and through the angle $\frac{\pi}{4}$, if $a = b$
13. Show that the origin is within the triangle whose angular points are (2,1), (3, -2) and (-4, 1)
14. Show that the line joining the points A (+6, -7, 0) and BC (16, -19, -4) intersects the line joining the points P(0,3,-6) and Q (2,-5, 10) at the point (1,-1,2)
15. Find the derivative of $\tan 2x$ from the first principles
16. A point P is moving with uniform velocity 'V' along a straight line AB. θ is a point on the perpendicular to AB at A and at a distance 'l' from it. Show that the angular velocity of P about θ is
17. State and prove the Eulers theorem on homogeneous functions.

SECTION - C

5 x 7 = 35 marks

18. Find the orthocentre of the triangle whose vertices are (5,-2), (-1,2) and (1,4)
19. Show that the area of the triangle formed by the lines $ax^2 + 2\gamma xy + by^2 = 0$ and $lx+my+n = 0$ is $\frac{n^2 \sqrt{h^2 - ab}}{am^2 - 2\gamma ln + bl^2}$

20. Find the angle between the lines joining the origin to the points of intersection of the curve $x^2 + 2xy + y^2 + 2x + 2y - 5 = 0$ and the line $3x - y + 1 = 0$
21. If a ray makes angle $\alpha, \beta, \gamma,$ and δ with the four diagonals of a cube, show that $\cos^2\alpha + \cos^2\beta + \cos^2\gamma + \cos^2\delta = \frac{4}{3}$
22. If $x^{\log y} = \log x$ then prove that $\frac{dy}{dx} = \frac{y}{x} \frac{(1 - \log x \log y)}{(\log x)^2}$
23. Show that the semi-vertical angle of the right circular cone of a maximum volume and of given slant height is $\tan^{-1} \sqrt{2}$
24. If the tangent at any point on the curve $x^{2/3} + y^{2/3} = a^{2/3}$ intersects the co-ordinate axis in A,B, then show that the length AB is constant.

